Tuning the lateral leakage loss of TM-like modes in shallow-etched waveguides using liquid crystals

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We examine the tuning effect a liquid crystal (LC) cladding has on the lateral leakage loss of TM-like modes in shallow-etched waveguides. For such waveguides with an air cladding, the guided TM-like mode and the unguided cladding TE-like mode can only be phase matched at precisely one angle. We find that for an anisotropic cladding such as an LC, this phase matching is now possible for a range of angles. Each of these angles corresponds to a given orientation of the molecules in the LC cladding. We show that the waveguide width at which the minimum in leakage loss occurs can be changed by varying the orientation of the LC cladding. We find different tuning regimes, identify a suitable tuning range, and discuss the feasibility of tunable leakage loss experiments. © 2014 Optical Society of America

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1. Introduction
Silicon-on-insulator (SOI) waveguides possess many desirable properties that make them suitable for high-density integration on a single chip. SOI technology has been very successful because it utilizes a high index contrast material system [1] and is compatible with complementary metal–oxide–semiconductor (CMOS) fabrication technology (i.e., it is cheap). An interesting class of SOI waveguides is the quasi-planar shallow-etched waveguide [2–4], which is suitable for active SOI devices such as modulators and/or light-emitting sources. Unfortunately, for certain practical geometries, the TM-like mode of these waveguides exhibits lateral leakage loss. The effective index of the guided TM-like mode of the waveguide is less than that of the radiating (cladding) slab TE-like mode. This slab TE-like mode can propagate in any direction since it is unguided and can be phase matched to the guided TM-like mode for a particular angle. Consequently, the guided TM mode suffers from lateral leakage loss since it can be phase matched to a radiating mode.

Recently in the literature, the existence of this leakage loss and its dramatic dependence on the width of the waveguide has been observed experimentally [5] for straight waveguides. In [6], lateral leakage loss in shallow-etched bent waveguides is analyzed. Here the lateral leakage is shown to depend on both the bend radius and the waveguide width. In other studies [7,8] a waveguide structure with a dimple at its center is proposed. It is then shown that such a structure is both low loss and fabrication tolerant. Reference [9] proposes a structure wherein two waveguides are parallel to each other.
Depending on the gap between the two waveguides, the leakage loss can be canceled when both waveguides are excited with quadrature phase.

So far, previous studies have been limited in terms of controlling the lateral leakage loss in shallow-etched waveguides. For a waveguide at a constant temperature, with no applied voltage and no stress, the effective indices of each of the modes in the waveguide are fixed. The leakage properties of the waveguide are then also fixed since they arise from the interplay between the effective indices. If we can modulate the effective indices of the waveguide modes, then we would also modulate the leakage loss of the waveguide. In practice this can be done by thermo-optics or electro-optics. In silicon, the thermo-optic effect is large enough for practical applications compared to the electro-optic effect. Consequently, temperature tuning is often considered for tuning SOI waveguides, but this requires constant power supply, and the tuning range is limited. A material with a high electro-optic effect can be integrated with silicon in order to tune it electro-optically. An example of such a material is a liquid crystal (LC). LCs have excellent electro-optic properties. Their large electro-optic coefficient has established them as the material of choice in display applications. However, they are also suitable for nondisplay applications. They have been used for different tunable photonic components such as spatial light modulators, lasers, filters, switches, and nonlinear components. Many groups have proposed designs in which LCs are used to alter the properties of waveguides. The LC can be used as a tunable cladding material or as the guiding medium.

We propose a structure in which a nematic LC layer is used as the upper cladding of a conventional shallow-etched waveguide. The orientation of the LC in the cladding can be changed by the application of a moderate voltage. This change in orientation is accompanied by a change in the cladding index felt by the modes in the waveguide and results in a change in the effective index of these modes. Since the lateral leakage loss arises from the interplay of these effective indices, this causes a change in the leakage loss of the waveguide.

2. Lateral Leakage Loss Mechanism

Before proceeding any further, a brief review of the mechanism for lateral leakage loss is in order. The optical fields in an SOI shallow-etched waveguide are confined in the y direction by the index mismatch between air, silicon, and silica (see Fig. 1). In the x direction, confinement is provided by the step discontinuity in silicon. As it travels along the waveguide, the TE-like (resp. TM-like) mode gets additional small $E_x$ and $E_y$ (resp. $H_x$ and $H_y$) components at the waveguide boundaries. Consequently, we have TE-like and TM-like modes in such waveguides, with TE–TM (and TM–TE) mode conversion occurring at the waveguide walls. Mode conversion can lead to lateral leakage loss if certain conditions are satisfied. In each case, we must examine the graph in Fig. 2 to determine which modes are evanescent in the cladding and hence determine which mode suffers from lateral leakage loss.

For a TE-like propagating shallow-etched waveguide mode, the TE field must necessarily be laterally evanescent in the shallow-etched waveguide cladding. In general, the propagation constant of the TM-like mode in a slab waveguide with thickness $t_2$ is lower than that of the TE-like mode in the waveguide. Hence TM fields resulting from TE–TM mode conversion are evanescent. Consequently, the TE-like modes show no lateral leakage loss.

For a TM-like propagating shallow-etched waveguide mode, the TM field in the cladding must be evanescent as well. However, the propagation constant of the TE-like mode in a slab waveguide with thickness $t_2$ is larger than that of the TM-like mode in the waveguide. Hence TE fields that arise due to TM–TE conversion at the ridge boundary are not evanescent. These TE fields can be phase matched to a TE slab mode propagating laterally at angle $\theta$ in the slab region. Consequently, the TM-like mode in these waveguides exhibits lateral leakage loss.

Consider a TM-like mode propagating in a shallow-etched waveguide (see Fig. 2). At the right waveguide boundary, it generates transmitted and reflected TE waves that have a relative phase of $\pi$. The reflected TE wave travels through the waveguide core at an angle to the z axis since it is not
guided. When it gets to the left waveguide boundary, the guided TM-like mode again generates transmitted and reflected TE waves with a relative phase of $\pi$. The new transmitted TE wave combines with the previously reflected TE wave. If the phase accumulated by the previously reflected TE wave as it travels through the waveguide core is a multiple of $2\pi$, then it will interfere destructively with the newly transmitted TE wave. We can write this condition as follows:

$$\beta_{TM} \cdot D - k_{TE}^{(core)} \cdot \sqrt{D^2 + W^2} = 2m\pi. \quad (1)$$

Here $m$ is a positive integer. After some simple algebra, we arrive at the well-known expression for the resonance condition of the leakage loss of SOI shallow-etched waveguides:

$$W = \frac{m\lambda}{\sqrt{N_{eff.TE}^{(core)} - N_{eff.TM}^2}}. \quad (2)$$

where $\lambda$ is the wavelength of the light in the waveguide, $N_{eff.TM}$ is the effective index of the guided TM-like waveguide mode, and $n_{eff.TE}^{(core)}$ is the effective index of the (unguided) TE wave that traverses the waveguide core.

3. Tuning the Lateral Leakage Loss of the TM-like Mode

For a shallow-etched waveguide with air cladding [5–9], the TE and TM modes feel the same refractive index in the cladding. When LC is used as the upper cladding layer, the situation becomes far more interesting. The LC can be oriented such that the TE and TM modes in the waveguide feel a different refractive index in the cladding [14]. In this way it is possible to change the effective index of the TE and TM modes separately; this is equivalent to changing $n_{eff.TE}^{(core)}$ and/or $N_{eff.TM}$ in Eq. (2) from the values they had when the waveguide had an air cladding. If this is the case, the resonance condition can be fulfilled if $W = W_{LC}$, which will in general be different from $W_{air}$.

There are three main possibilities for orienting the LC in the cladding. First, orient the LC along the $x$ axis; the TE and TM modes feel the extraordinary ($n_e$) and ordinary ($n_o$) indices of the LC in the cladding, respectively. Second, we could orient the LC along the $y$ axis; the TE and TM modes would feel an index $n_o$ and $n_e$ in the cladding, respectively. Third, we could orient the LC along the $z$ axis. In this case, both modes only feel the ordinary index ($n_o$) of the LC in the cladding. We can choose any of the three states above as the initial state of the LC and then choose one from the remaining two as the final state of the LC. We choose an LC layer as in options 1 and 2 above as the initial and final states. For this combination we would see the largest change in the effective indices and hence leakage loss of the waveguide.

It is instructive to take a look at the $k$-vector diagram for a waveguide with an anisotropic upper cladding. Figure 4 shows $k$-vector diagrams of the fundamental TE and TM modes and the radiating cladding TE mode, for an air cladding and for claddings as in options 1 and 2 above. Given that the TE and TM modes feel an index $n_o$ or $n_e$ depending on the LC alignment, we can make the following observations. The propagation constant of the TM mode in Fig. 4(c) is greater than that in Fig. 4(b).
On the other hand, the propagation constant of the TE mode in Fig. 4(b) is greater than that in Fig. 4(c). Finally, the unguided TE slab mode propagation constant \(k_{\text{TE}}^{\text{clad}}\) is not the same in every direction for a cladding made out of LC aligned along the \(x\) axis. In this case the refractive index felt by this mode in the cladding is given by

\[
n(\theta) = \frac{1}{\sqrt{\left(\frac{\cos \theta}{n_{y}}\right)^2 + \left(\frac{\sin \theta}{n_{z}}\right)^2}}.
\]  

(3)

In Fig. 4(b) the tip of \(k_{\text{TE}}^{\text{clad}}\) traces out a quadrant of an ellipse rather than that of a circle [Figs. 4(a) and 4(c)]. It is this anisotropy in cladding index that makes the tuning possible. In previous studies with an air cladding, \(\beta_{\text{TM}}\) and \(k_{\text{TE}}^{\text{clad}}\) can only be phase matched at precisely one angle. When an LC cladding is used, they can now be phase matched for a range of angles. Each of these angles corresponds to a given orientation of the LC in the cladding. By varying the orientation of the LC in the cladding, it is then possible to vary the waveguide width at which the minima in leakage loss occur.

In order to confirm the qualitative arguments given above, we consider two waveguide geometries: (i) \(t_1 = 205 \text{ nm}, \ t_2 = 190 \text{ nm}\) and (ii) \(t_1 = 220 \text{ nm}, \ t_2 = 150 \text{ nm}\). For each of these geometries, we calculate the effective index of the TM mode for waveguide widths between 500 and 2500 nm. We also calculate the effective index of the TE mode in a slab waveguide with thickness \(t_1\). We do this for the three cases in Fig. 4. The operating wavelength is 1.55 \(\mu\text{m}\), and we only consider the fundamental waveguide modes. The refractive indices of the core and cladding of the waveguide are \(n_{\text{core}} = 3.475\) and \(n_{\text{clad}} = 1.444\), respectively. For the LC upper cladding, we use the LC E7 \((n_x = 1.7, n_y = 1.5\) for a wavelength of 1.55 \(\mu\text{m}\)). For cladings as in Figs. 4(a) and 4(c), there is no need to take into account the orientation of the unguided TE wave in the waveguide core. For a cladding as in Fig. 4(b), the calculation is more involved. We first compute the effective index of the TM mode for each waveguide width. Next, we obtain the effective index of the TE mode in a slab waveguide of thickness \(t_1\); we do this for all possible directions of the TE mode in the \(x-z\) plane. For each width, the correct value of \(n_{\text{eff,TE}}\) is obtained by solving Eq. (4) for self-consistency:

\[
\cos(\theta) = \frac{N_{\text{eff,TM}}(W)}{n_{\text{eff,TE}}(\theta),}
\]  

(4)

For each waveguide width we now have corresponding \(n_{\text{eff,TE}}^{\text{core}}\) and \(N_{\text{eff,TM}}\). We can make a guess of the waveguide width for which we have the first minimum in leakage loss, by plugging these values into Eq. (2) and looking for the combination of values that yield an \(m\) closest to 1. We perform these calculations for each type of upper cladding. The results are tabulated below in Table 1.

We now turn our attention to calculating actual loss values for the geometries considered earlier. In order to do this, we employ full vectorial finite element simulations. The intent here is to verify that we indeed have tuning and ascertain the extent of this tuning. We use the fully anisotropic finite-element-based mode solver in COMSOL Multiphysics. We consider waveguide widths between 500 and 2500 nm. We simulate the two cases considered earlier, i.e., (i) \(t_1 = 205 \text{ nm}, \ t_2 = 190 \text{ nm}\), and (ii) \(t_1 = 220 \text{ nm}, \ t_2 = 150 \text{ nm}\). The refractive indices of the silicon core and silica cladding of the waveguide are \(n_{\text{core}} = 3.475\) and \(n_{\text{clad}} = 1.444\), respectively, and the operating wavelength is 1.55 \(\mu\text{m}\).

Case 1 corresponds to the geometry considered in previous works [5–9], and the second case corresponds to a geometry that is in the process of being fabricated. The simulation results for case 1 are shown in Fig. 5.

The simulation for an air cladding (red curve) is in excellent agreement with previous results [7]. The loss minima occur at waveguide widths of 711, 1431, and 2154 nm. When we use LC in the cladding of the waveguide, the loss minima are shifted as expected. As mentioned before, we start out with a situation in which the LC in the cladding is oriented along the \(x\) axis and then transition to one in which it is oriented along the \(y\) axis. For a waveguide with LC upper cladding, the lateral leakage loss still follows a cyclic pattern. The waveguide width at which

<table>
<thead>
<tr>
<th>(\Delta t [\text{nm}])</th>
<th>(W_{\text{Air}} [\text{nm}])</th>
<th>(W_{\text{LC,x}} [\text{nm}])</th>
<th>(W_{\text{LC,y}} [\text{nm}])</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>708</td>
<td>759</td>
<td>794</td>
</tr>
<tr>
<td>70</td>
<td>694</td>
<td>751</td>
<td>819</td>
</tr>
</tbody>
</table>

"This gives a guess of the width at which the first minimum in leakage loss would occur. The step height for each geometry is given by, \(\Delta t = t_1 - t_2\)."
the minimum in the leakage loss occurs can be tuned by at least 35 nm—from 760 to 795 nm. According to our simulations, we can change the leakage loss at a width of 795 nm, from 2 to about 0 dB/cm, by switching the LC from being oriented along the x axis to the y axis, respectively.

Case 2 is for a structure that is in the process of being fabricated and for which we intend to perform loss measurements. Here the step height is more than doubled compared to the previous case. We expect a larger modulation of the leakage loss for a fixed waveguide width using the LC cladding. The lateral leakage loss curves for this case are shown in Fig. 6. We notice that the maximum of the leakage loss has increased by about one order of magnitude as expected. For air cladding, the loss minima occur at widths of 722, 1469, and 2212 nm. When an LC cladding is used, we predict that it would be possible to shift the position of the leakage loss minima by 28 nm, from a width of 776 to 804 nm. This time for an 804 nm wide waveguide, the leakage loss can be changed from 19 to 0 dB/cm by switching the LC from being oriented along the x axis to the y axis, respectively. The change in leakage loss for case 2 is about 10 times larger than that for case 1. This large change in leakage loss makes an experimental realization very feasible.

Table 2 summarizes the values of the waveguide width at which the first minimum in the loss curves in Figs. 5 and 6 occur. We can now determine the accuracy of our earlier guess. For case 1, our guess is excellent; it is accurate to within 0.4% in the worst case, i.e., the air cladding. On the other hand, for case 2, the guess is not that good; in the best case (LC oriented along the y axis in the cladding), it is only accurate to within 1.8%. This discrepancy is due to the difference in step height between both cases. The accuracy of our guess deteriorates with increasing step height. We confirm this by performing simulations for waveguide geometries with step heights between 15 and 70 nm.

4. Wavelength Dependence of the Leakage Loss

From Eq. (2), it is evident that for a fixed waveguide width, the lateral leakage loss is also wavelength dependent. This has already been investigated for bent shallow-etched waveguides [7]. In what follows, we look at the wavelength dependence of the lateral leakage loss when an LC cladding is used as the upper cladding of a shallow-etched waveguide.

We perform the same simulations as in the previous section, only this time we vary the wavelength from 1.5 to 1.6 μm. For simplicity, we neglect the dispersion of the LC over this wavelength range. Figures 7 and 8 show the variation of the lateral

![Fig. 6. Leakage loss of the fundamental TM mode for a waveguide with $t_1 = 220$ nm, $t_2 = 150$ nm. The loss minima occur at 722, 1469, and 2212 nm. When LC oriented along the x axis is used as cladding the loss minima shift to 776, 1579, and 2378 nm. After switching the LC, the loss minima shift to 804, 1642, and 2476 nm.](image1)

![Fig. 7. Leakage loss of the fundamental TM mode for a waveguide with $t_1 = 220$ nm, $t_2 = 150$ nm and LC cladding. The LC is oriented along the x axis. The color map is the logarithm (base 10) of the leakage loss.](image2)

![Fig. 8. Leakage loss of the fundamental TM mode for a waveguide with $t_1 = 220$ nm, $t_2 = 150$ nm and LC cladding. The LC is oriented along the y axis. The color map is the logarithm (base 10) of the leakage loss.](image3)

### Table 2. Upper Part, Waveguide Widths at which the First Minimum in the Loss Curve Occurs; Lower Part, Error between the Predicted Widths in Table 1 and Those in the Upper Part of this Table

<table>
<thead>
<tr>
<th>$\Delta t$ [nm]</th>
<th>$W_{Air}$ [nm]</th>
<th>$W_{LC,x}$ [nm]</th>
<th>$W_{LC,y}$ [nm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>711</td>
<td>760</td>
<td>795</td>
</tr>
<tr>
<td>70</td>
<td>722</td>
<td>776</td>
<td>804</td>
</tr>
<tr>
<td>15</td>
<td>0.4%</td>
<td>0.1%</td>
<td>0.1%</td>
</tr>
<tr>
<td>70</td>
<td>4.0%</td>
<td>3.3%</td>
<td>1.8%</td>
</tr>
</tbody>
</table>

*The step height for each geometry is given by $\Delta t = t_1 - t_2$. 

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![Fig. 5](image4)
leakage loss with both the waveguide width and the wavelength. The logarithm to the base 10 of the lateral leakage loss is used as the color map for these 2D plots. Overall we notice a significantly stronger dependence of the leakage loss on the waveguide width than on the wavelength. Nevertheless, for the range of waveguide widths close to the leakage loss minima, there is a strong dependence on the wavelength. In this range of widths the leakage loss varies by about 10 dB/cm on average with the wavelength. This is an important effect that should be taken into account in practice.

5. Discussion
In the previous sections, we made some interesting predictions about how the leakage loss of a shallow-etched SOI waveguide with upper LC cladding would change if the LC is switched. We now proceed to discuss factors that could limit the predicted change in leakage loss. Accordingly, we address the effect of additional losses from the LC layer and waveguide line width variation on the change in lateral leakage loss of the waveguide.

The LC upper cladding layer can induce additional losses from the waveguide. These can be either scattering or absorption losses. In the nematic state and for the wavelength range considered, the scattering loss can be two orders of magnitude stronger than the absorption loss [20]. Scattering losses arise from a lack of homogeneity in the alignment of the LC molecules above the waveguide. This loss can be reduced by forcing all the molecules in the LC layer above the waveguide to be aligned in a particular direction [14]. If a voltage is then applied to the LC layer, the change in orientation would be homogeneous, thus reducing scattering losses once more. Absorption losses, on the other hand, are intrinsic to the LC material and would vary depending on the kind of LC used. For E7, the total optical loss (i.e., scattering and absorption) is about 1 cm\(^{-1}\) at 1550 nm [20]. This corresponds to the imaginary part of the refractive index proportional to 10\(^{-5}\). We added this loss to the LC cladding in our simulation. The result is an increase of about 2.5 dB/cm in lateral leakage loss compared to the case in which the LC has no loss. Although the LC layer increases the total loss of the waveguides, the change in leakage loss remains the same. For case 2, and a waveguide width of 804 nm, the leakage loss for LC oriented along the x and y axes is 21.7 and 2.5 dB/cm, respectively, giving a change in loss of 19.2 dB/cm. We zoom in around waveguide widths between 750 and 820 nm and plot the leakage loss for LC with and without loss. This plot is shown in Fig. 9.

Selvaraja et al. [21] report SOI waveguide line-width uniformity <0.6 nm within a chip and <2 nm between chips in experiments. Let us assume the worst case. If the target waveguide width is 804 nm but we get either 806 or 802 nm, then the change in loss for LC reorienting from being aligned along x to being aligned along y would be 22 and 16.9 dB/cm, respectively. Furthermore, even if the target waveguide width is 5 nm off, i.e., 809 or 799 nm, the change in loss would still be 25.6 and 12.8 dB/cm, respectively. Consequently, our prediction of a lateral leakage loss tuning range of 28 nm is indeed realizable.

6. Conclusion
We propose a method to tune the lateral leakage loss of the TM-like mode in shallow-etched SOI waveguides. We consider a shallow-etched waveguide with LC upper cladding. The effects of the LC cladding on the modes of the waveguide are explained. It is shown that the lateral leakage loss can be modulated by changing the orientation of the LC in the cladding. This change in orientation can be obtained by the application of a moderate voltage. Two different waveguide structures are considered, and the lateral leakage loss is shown to increase with increasing step height. We predict that the largest modulation of the leakage loss can be observed by having a structure in which the LC is initially oriented along the x axis and subsequently oriented along the y axis. We show that our proposal is an electrically controllable switch for the leakage loss of a shallow-etched waveguide with a particular width. We also discuss the most important factors that could limit the predictions we make for change in leakage loss and come to the conclusion that the predicted change in leakage loss is experimentally achievable.

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References


